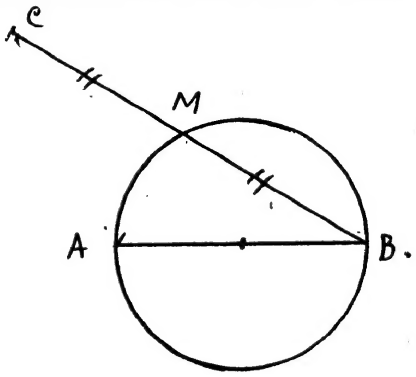
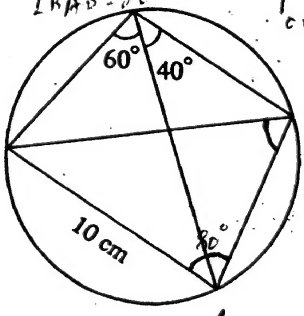
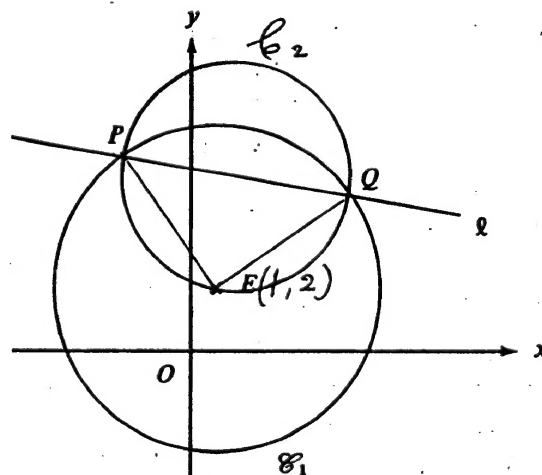


Solution	Marks	Remarks
<p>1. (a) Increase percentage = $(\frac{1000}{8000} \times 100)\%$ $= 12.5\%$</p> <p>(b) His savings = $\\$9000 \times \frac{3}{10}$ $= \\$2700$</p>	<p>1A</p> <p>$\frac{1A}{2}$</p> <p>1A</p> <p>$\frac{1A}{2}$</p>	<p>for $\frac{1000}{8000}$</p> <p>Accept 12.5</p>
<p>2. (a) $x + 1 > \frac{1}{5}(3x + 2)$ $5x - 3x > 2 - 5$ $2x > -3$ $x > -\frac{3}{2}$</p> <p>(b) Furthermore, if $-4 \leq x \leq 4$, then the range of x is $-\frac{3}{2} < x \leq 4$.</p>	<p>1M</p> <p>$\frac{1A}{2}$</p> <p>2A</p> <p>$\frac{2}{2}$</p>	<p>OR</p> <p>$x - \frac{3}{5}x > \frac{2}{5} - 1$ 1M</p> <p>$\frac{2}{5}x > -\frac{3}{5}$</p> <p>$x > -\frac{3}{2}$ 1A</p> <p>-1 if '=' incorrect Accept graphical representation</p>
<p>3. (a) Since $(x + 1)$ is a factor of $x^4 + x^3 - 8x + k$, $(-1)^4 + (-1)^3 - 8(-1) + k = 0$ <i>omit pp1</i> $k = -8$</p> <p>(b) $x^4 + x^3 - 8x - 8 = (x + 1)(x^3 - 8)$ $= (x + 1)(x - 2)(x^2 + 2x + 4)$</p> <p>OR $(2)^4 + (2)^3 - 8(2) - 8 = 0$ $\rightarrow x - 2$ is another factor $\therefore x^4 + x^3 - 8x - 8 = (x + 1)(x - 2)(x^2 + 2x + 4)$ <i>pp1</i></p>	<p>1M</p> <p>$\frac{1A}{2}$</p> <p>1M+1A</p> <p>1A+1A</p> <p>$\frac{4}{4}$</p> <p>1A+2A</p>	<p>1M for $(x+1) \times$ cubic exp.</p> <p>1A for $x^3 - 8 = (x-2)(x^2+2x+4)$</p> <p>1M for $(x+1)(x-2) \times$ quadratic exp.</p>

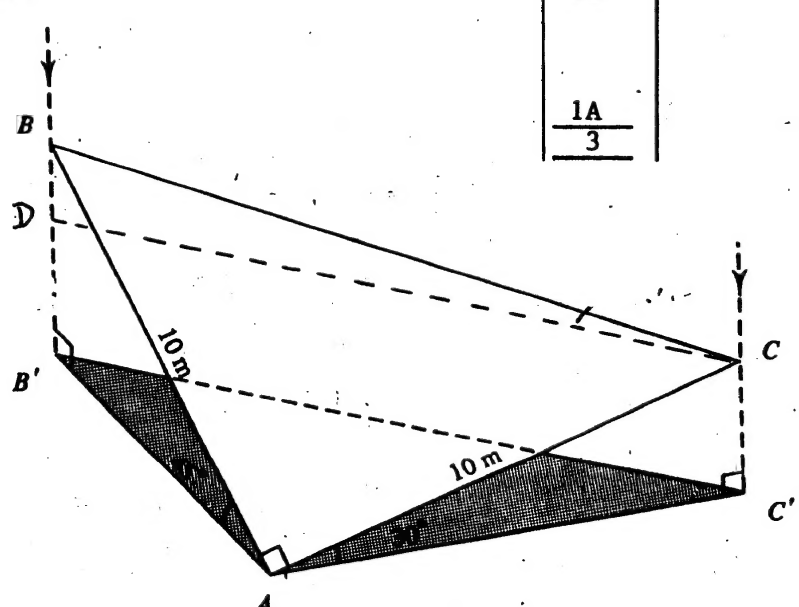
Solution	Marks	Remarks
<p>4. (a) </p> <p>(b) Consider $\triangle ABM$ and $\triangle ACM$ (OR joining AM, AC)</p> <p>Since AB is a diameter, $\angle AMB = 90^\circ$ (OR $\angle AMB = \angle AMC$) $\angle AMB = \angle AMC$ As AM is common and $BM = MC$, the two triangles are congruent. (SAS) $\therefore \angle BAM = \angle CAM$, i.e. AM bisects $\angle BAC$.</p>	<p>1A</p> <p><u>1A</u> 2</p> <p>1</p> <p>1</p> <p>1</p> <p><u>1</u> 4</p>	<p>For circle with A,B,M</p> <p>Indication of $BM = MC$</p> <p>In this part, candidates are expected to give brief reasons.</p> <p>State $\triangle AMB \cong \triangle AMC$ (with reason) conclude AM bisects $\angle BAC$</p>
<p>5. (a) $\begin{cases} x + 2y = 5 & \dots\dots\dots (i) \\ 5x - 4y = 4 & \dots\dots\dots (ii) \end{cases}$</p> <p>$2 \times (i) + (ii) \Rightarrow 7x = 14$ $x = 2$</p> <p>Putting $x = 2$ in (i), $2y = 3$ $y = \frac{3}{2}$</p> <p>\therefore the solution is $\begin{cases} x = 2 \\ y = \frac{3}{2} \end{cases}$</p> <p>(b) By (a), $\frac{a}{c} = 2$ and $\frac{b}{c} = \frac{3}{2}$ $a : b : c = 4 : 3 : 2$ (or equivalent ratios)</p>	<p>1M</p> <p>1A</p> <p>1A</p> <p><u>3</u></p> <p>2A 2M</p> <p><u>2A 1A</u> 3</p>	<p>For elim. or subs.</p>
<p>6. (a) $\angle ABD (= \angle ACD) = 60^\circ$</p> <p>Since ABCD is a cyclic quadrilateral, $\angle BAD + \angle BCD = 180^\circ$ $\therefore \angle BAD = 180^\circ - (60 + 40)^\circ$ $= 80^\circ$</p> <p>(b) By the sine rule, $\frac{10}{\sin 60^\circ} = \frac{BD}{\sin 80^\circ}$ $BD = \frac{10 \sin 80^\circ}{\sin 60^\circ}$ $= 11.37 \text{ cm (corr. to 2 d.p.)}$</p>	<p>1A</p> <p><u>1A</u> 3</p> <p>1M+1A</p> <p><u>1A</u> 3</p>	<p>$\angle BDA = 40^\circ$</p> <p>$\angle BAD = 80^\circ$</p> <p></p>

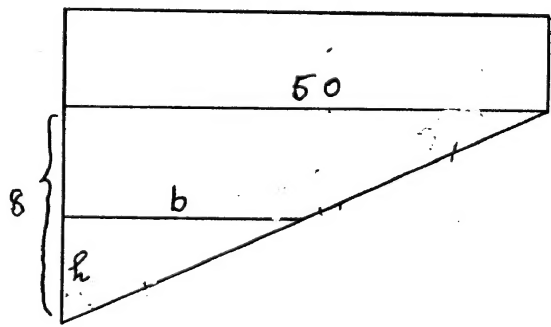
Solution	Marks	Remarks
<p>7. $3\tan\theta = 2\cos\theta$</p> <p>$3 \frac{\sin\theta}{\cos\theta} = 2\cos\theta$</p> <p>$3\sin\theta = 2\cos^2\theta$</p> <p>$3\sin\theta = 2(1 - \sin^2\theta)$</p> <p>$\therefore 2\sin^2\theta + 3\sin\theta - 2 = 0$</p> <p>$(2\sin\theta - 1)(\sin\theta + 2) = 0$</p> <p>$\sin\theta = \frac{1}{2}$ or -2 (rejected)</p> <p>The solutions are $\theta = 30^\circ$ or 150° ($\frac{\pi}{6}$ or $\frac{5\pi}{6}$) [as $\cos 30^\circ$ and $\cos 150^\circ \neq 0$].</p>	<p>1M</p> <p>1M</p> <p>1A</p> <p>1A</p> <p>1A</p> <p>1A+1A</p> <hr/> <p>7</p>	<p>Accept '$\sin\theta = \frac{1}{2}$' or '$\sin\theta = -2$'</p> <p>Deduct 1 for each extraneous solution.</p>

Solution	Marks	Remarks
8. (a) $E = (1, 2)$	$\frac{1A}{1}$	$E = 1, 2$ pp-1
(b) From $x + 7y - 40 = 0$, we have $x = 40 - 7y$ (or $y = \frac{40 - x}{7}$)		
Putting in \mathcal{C}_1 , $(40 - 7y)^2 + y^2 - 2(40 - 7y) - 4y - 20 = 0$	1M	
$50y^2 - 550y + 1500 = 0$	1A	
$y^2 - 11y + 30 = 0$ (or $x^2 - 3x - 10 = 0$)		
$(y - 5)(y - 6) = 0$		
$y = 5$ or 6 (or $x = 5$ or -2)	1A	$y = 5$ and $y = 6$ pp-1
$x = 5$ or -2		
$\therefore P = (-2, 6), Q = (5, 5)$	1A	Accept $P = (5, 5)$ $Q = (-2, 6)$
	$\frac{4}{4}$	
(c) \mathcal{C}_2 is given by $\frac{y - 6}{x + 2} \cdot \frac{y - 5}{x - 5} = -1$	1M+1A	OR Ctr. of $\mathcal{C}_2 = (\frac{3}{2}, \frac{11}{2})$ } 1A
i.e. $x^2 + y^2 - 3x - 11y + 20 = 0$	1A	radius = $\frac{5\sqrt{2}}{2}$ (=3.54)
		Eq. of \mathcal{C}_2 : $(x - \frac{3}{2})^2 + (y - \frac{11}{2})^2 = \frac{50}{4}$ }
		Answer 1M+1A
	$\frac{3}{3}$	
(d) Putting $(x, y) = (1, 2)$ in L.H.S. of \mathcal{C}_2	1M	OR Slope of PE x slope of
$1^2 + 2^2 - 3(1) - 11(2) + 20 = 0$	1A	$QE = -1$
$\therefore \mathcal{C}_2$ passes through E		
(As PQ is a diameter of \mathcal{C}_2), $\angle PEQ = 90^\circ$	1M)	OR Let $P = (-2, 6), Q = (5, 5)$
(Since $PE = QE$ (radii of \mathcal{C}_1)))	Slope of PQ = $-\frac{1}{7}$
$\angle EPQ = \frac{90^\circ}{2} = 45^\circ$)	Slope of PE = $-\frac{4}{3}$
	1A)	$\tan \angle EPQ = \frac{-\frac{1}{7} - \frac{-4}{3}}{1 + \frac{1}{7} \times \frac{4}{3}}$ 1M
		$= 1$
		$\angle EPQ = 45^\circ$ 1A
		OR $171.87^\circ - 126.87^\circ$ 1M
		$= 45^\circ$ 1A
	$\frac{4}{4}$	

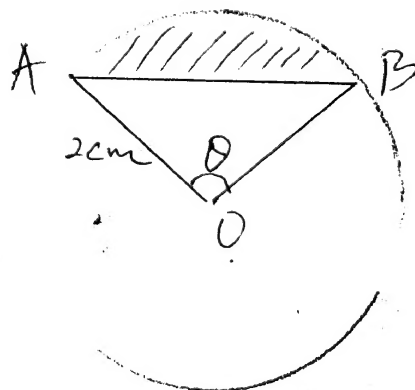


Solution	Marks	Remarks
<p>9. (a) $\frac{k}{1} = \frac{1}{k}$ $k^2 = \frac{1}{2}$ $k = \frac{1}{\sqrt{2}}$ (or $\frac{\sqrt{2}}{2}$) (as $k > 0$)</p>	<p>1M</p> <p>1A</p> <p><u>2</u></p>	<p>Do not accept $\pm \frac{1}{\sqrt{2}}$ but follow through</p>
<p>(b) $T(n) = \left(\frac{1}{\sqrt{2}}\right)^{n-1}$ [or $\frac{1}{(\sqrt{2})^{n-1}}$, $2^{-\frac{n-1}{2}}$, etc.]</p>	<p>1M+1A</p> <p><u>2</u></p>	<p>$\frac{1}{\sqrt{2}}^{n-1}$ p.p.</p>
<p>(c) Sum to infinity = $\frac{1}{1 - \frac{1}{\sqrt{2}}}$ $= \frac{\sqrt{2}}{\sqrt{2} - 1}$ $= \frac{\sqrt{2}(\sqrt{2} + 1)}{(\sqrt{2} - 1)(\sqrt{2} + 1)}$ $= 2 + \sqrt{2}$</p>	<p>1M+1A</p> <p>1M</p> <p><u>1A</u></p> <p><u>4</u></p>	
<p>(d) No. of terms in the product = $\frac{2n - 1 - 1}{2} + 1 = n$</p> <p>$T(1) \times T(3) \times T(5) \times \dots \times T(2n-1)$ $= 1 \times \frac{1}{2} \times \frac{1}{4} \dots \times \left(\frac{1}{\sqrt{2}}\right)^{2n-2}$ [or $1 \times \frac{1}{(\sqrt{2})^2} \times \frac{1}{(\sqrt{2})^4} \times \dots \times \frac{1}{(\sqrt{2})^{2n-2}}$] $= 1 \times \frac{1}{2} \times \frac{1}{2^2} \times \dots \times \frac{1}{2^{n-1}}$ $= \frac{1}{2^{1+2+\dots+(n-1)}}$</p> <p>$= \frac{1}{2^{\frac{n(n-1)}{2}}}$ [or $2^{\frac{-n(n-1)}{2}}$, etc.]</p>	<p>1A</p> <p>1M</p> <p>1M+1A</p> <p><u>4</u></p>	<p>1M for summing index as A.P.</p>

Solution	Marks	Remarks
<p>10. (a) $AB' = 10\cos 45^\circ$ $= 5\sqrt{2}\text{m}$ (or $\frac{10}{\sqrt{2}}$), (7.07107) $AC' = 10\cos 30^\circ$ $= 5\sqrt{3}\text{m}$ (8.66025)</p>	<p>1A</p> <p><u>1A</u> <u>2</u></p>	<p>Any figure roundable to 7.07</p>
<p>(b) $BC = \sqrt{10^2 + 10^2}$ $= 10\sqrt{2}\text{m}$ (14.14214) $BB' = 10\sin 45^\circ$ $= 5\sqrt{2}\text{m}$ (7.07107) $CC' = 10\sin 30^\circ$ $= 5\text{m}$</p>	<p>1A</p> <p>1A</p> <p><u>1A</u> <u>3</u></p>	<p>No unit - 1 mark for u.s. paper u - 1</p>
		
<p>(c) Let D be the foot of the perpendicular from C to BB'. $BD = (5\sqrt{2} - 5)\text{m}$ (=2.07107) $B'C' = CD$ $= \sqrt{(10\sqrt{2})^2 - (5\sqrt{2} - 5)^2}$ $= \sqrt{125 + 50\sqrt{2}}\text{m}$ (= 13.9897)</p>	<p>1M</p> <p>1M</p> <p>1A</p> <p><u>3</u></p>	<p>Accept figures roundable to 13.9 - 14.0</p>
<p>(d) By the cosine rule, $\cos B'AC' = \frac{50 + 75 - (125 + 50\sqrt{2})}{2 \times 5\sqrt{2} \times 5\sqrt{3}} (= -\frac{1}{\sqrt{3}}, -0.57735)$ $\angle B'AC' = 125^\circ$ (125.264)</p>	<p>1M</p> <p>1A</p>	<p>124° - 125°</p>
<p>Area of the shadow $= \frac{1}{2} \times 5\sqrt{2} \times 5\sqrt{3} \sin 125.264^\circ$ $= 25\text{m}^2$</p>	<p>1M</p> <p>1A</p> <p><u>4</u></p>	<p>For $\Delta = \frac{1}{2} ab \sin C$ 25.0 - 25.4</p>

Solution	Marks	Remarks
<p>11. (a) Area of cross-section = $\frac{50}{2} (2 + 10) = 300\text{m}^2$</p> <p>Vol. of water = $20 \times 300 = 6000\text{m}^3$</p>	<p>2CA 1M+1A</p>	<p>1M for Vol. = Area of cross-section \times width</p>
	<p>OR $\frac{20 \times 10 \times 2}{2} + \frac{1}{2} (10 \times 8) \times 20$</p>	
	2	
<p>(b) (i) When the depth of water at the deeper end is 8m, the cross-section of water is a triangle of area $\frac{8 \times 50}{2} = 200\text{m}^2$.</p> <p>Vol. of water left = $200 \times 20 = 4000\text{m}^3$.</p>	<p>2A</p>	<p>OR</p> <p>Drop in water level = 2m</p> <p>Water pumped out = $2 \times 50 \times 20 = 2000\text{m}^3$ 1A</p> <p>Water left = 4000m^3 1A</p>
<p>(ii) Vol. of water pumped out in 8 hours</p> <p>= $(0.125)^2 \pi \times 3600 \times 8 \times 3$</p> <p>= $1350\pi \text{ m}^3$</p> <p>= 4241m^3 (correct to the nearest m^3) (4241.15)</p>	<p>1M+1A</p> <p>1A</p>	<p>1M for area of cross-section</p>
<p>(iii) Vol. of water left after 8 hrs = $6000 - 4241$</p> <p>= 1759m^3</p>	<p>1M</p>	
<p>When the depths of water are 8m and h m, the corresponding cross-sections of water are two similar triangles with bases 50m and b m.</p> <p>$\frac{b}{h} = \frac{50}{8}$ or $b = \frac{50}{8} h$</p>	<p>1A</p>	
<p>$\therefore \frac{1}{2} b \times h \times 20 = 1759$</p>	<p>1M</p>	
<p>$\frac{20}{2} \times \frac{50}{8} h^2 = 1759$</p>	<p>1M</p>	
<p>$h = 5.305 = 5.3$ (correct to 1 d.p.)</p>	<p>1A</p> <p>10</p>	<p>$\left(\frac{h}{8}\right)^2 = \frac{1759}{4000}$</p>
		

Solution	Marks	Remarks																											
12. (a) (i) Area of $\triangle OAB = \frac{1}{2}(2)(2)\sin\theta = 2\sin\theta \text{ cm}^2$ ^{u-1}	1A																												
(ii) The area is greatest when $\theta = \frac{\pi}{2} \approx 1.57$	1A	90° not acceptable																											
	<u>2</u>																												
(b) Area of sector OAB = $\frac{1}{2}(2)^2\theta = 2\theta \text{ (cm}^2\text{)}$ ^{↑ optimal.}	1A																												
$2\theta - 2\sin\theta = 2$	1M																												
$\therefore \theta - \sin\theta - 1 = 0$	<u>1A</u>																												
	<u>3</u>																												
(c) $f(0) = 0 - 0 - 1 < 0$																													
$f(3) = 3 - \sin 3 - 1 (=1.859) > 0$	1M	For sub. $f(0)$, $f(3)$ Accept graphical method																											
$\therefore 0 < \alpha < 3$ ^{if wrong, 1A is not given.}	<u>1A</u>																												
^{if omitted, no 1A}	<u>2</u>																												
(d)																													
<table border="1"> <thead> <tr> <th>Interval</th><th>Mid-value θ</th><th>$f(\theta)$</th></tr> </thead> <tbody> <tr> <td>$0 < \alpha < 3$</td><td>1.5</td><td>-</td></tr> <tr> <td>$1.5 < \alpha < 3$</td><td>2.25</td><td>+</td></tr> <tr> <td>$1.5 < \alpha < 2.25$</td><td>1.875 (1.88)</td><td>-</td></tr> <tr> <td>$1.875 < \alpha < 2.25$</td><td>2.063 (2.06)</td><td>+</td></tr> <tr> <td>$1.875 < \alpha < 2.063$</td><td>1.969 (1.97)</td><td>+</td></tr> <tr> <td>$1.875 < \alpha < 1.969$</td><td>1.922 (1.92)</td><td>-</td></tr> <tr> <td>$1.922 < \alpha < 1.969$</td><td>1.946 (1.95)</td><td>+</td></tr> <tr> <td>$1.922 < \alpha < 1.946$</td><td></td><td></td></tr> </tbody> </table>	Interval	Mid-value θ	$f(\theta)$	$0 < \alpha < 3$	1.5	-	$1.5 < \alpha < 3$	2.25	+	$1.5 < \alpha < 2.25$	1.875 (1.88)	-	$1.875 < \alpha < 2.25$	2.063 (2.06)	+	$1.875 < \alpha < 2.063$	1.969 (1.97)	+	$1.875 < \alpha < 1.969$	1.922 (1.92)	-	$1.922 < \alpha < 1.969$	1.946 (1.95)	+	$1.922 < \alpha < 1.946$			1M+1A	1M Testing of sign at mid-value of suitable interval
Interval	Mid-value θ	$f(\theta)$																											
$0 < \alpha < 3$	1.5	-																											
$1.5 < \alpha < 3$	2.25	+																											
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$1.875 < \alpha < 2.063$	1.969 (1.97)	+																											
$1.875 < \alpha < 1.969$	1.922 (1.92)	-																											
$1.922 < \alpha < 1.969$	1.946 (1.95)	+																											
$1.922 < \alpha < 1.946$																													
	1M	1A Correct sign Correct choice of sub- interval																											
	1A																												
We see that α lies between 1.922 and 1.946.																													
$\therefore \alpha = 1.9$ (correct to 1 d.p.)	<u>1A</u>																												
	<u>5</u>																												



Solution	Marks	Remarks
<p>13. (a) Since $p + q = 1$,</p> <p>putting $p = 3q$</p> $4q = 1$ $q = \frac{1}{4}$	<p>1A</p> <p><u>1A</u> <u>2</u></p>	<p>optional</p> <p>only $q = \frac{1}{4}$ 2A.</p>
<p>(b) (i) The probability that the first ball drawn is black is $\frac{n}{10}$.</p> <p>After a black ball has been drawn, the probability of drawing a second black ball is $\frac{n-1}{9}$.</p> <p>\therefore the probability that both balls are black</p> $= \frac{n}{10} \times \frac{n-1}{9}$ $= \frac{n(n-1)}{90}$	<p>1A</p> <p>1A</p> <p>1M</p>	<p>$\frac{n}{10} \times \frac{n-1}{9}$ 1A+1A+1M.</p> <p>$\frac{n}{10} \times \frac{n-1}{10}$ 1A+1M.</p> <p>wrong.</p>
<p>(ii) $\frac{n(n-1)}{90} > \frac{1}{3}$</p> $3n^2 - 3n - 90 > 0$ $n^2 - n - 30 > 0$ $(n-6)(n+5) > 0$ <p>$\therefore n > 6$ or $n < -5$</p> <p>As n is integral and positive, $n = 7, 8, 9$ or 10.</p>	<p>1M</p> <p>1A</p> <p>1A</p> <p><u>1A</u> <u>7</u></p>	<p>Accept $n > 6$ with conv. $n < -5$</p> <p>by testing $n = 7, 8, 9, 10$ 3A</p> <p>all correct</p>
<p>(c) The probability that the first ball drawn is red and the second is also red = $\frac{1}{2} \times \frac{4}{6} (= \frac{1}{3})$.</p> <p>The probability that the first is green and the second is red = $\frac{1}{2} \times \frac{3}{6} (= \frac{1}{4})$.</p> <p>$\therefore$ the probability that the ball drawn from N is red = $\frac{1}{3} + \frac{1}{4} = \frac{7}{12}$.</p>	<p>1A</p> <p>1A</p> <p><u>1A</u> <u>3</u></p>	

no explicit
only expression.

Solution	Marks	Remarks
<p>14.</p> <p>(a).</p>	<p>1A</p> <p>+</p> <p>1A</p> <p>+</p> <p>1A</p>	<p>1A for each line</p> <p>± 1 horizontal/vertical unit at (100, 0), (0, 100); (20, 0), (60, 80); (0, 20), (100, 20)</p>
	1A	Region
	<u>4</u>	
<p>(b) (i) $z = 100 - x - y$</p> <p>(ii) Cost of mixture = $6x + 5y + 4z$ $= 6x + 5y + 4(100 - x - y)$ $= 2x + y + 400$ dollars</p> <p>(iii) $400x + 600y + 400z \geq 44\ 000$ $800x + 200y + 400z \geq 48\ 000$ Putting $z = 100 - x - y$, $y \geq 20$ $2x - y \geq 40$</p> <p>Further, (as $z \geq 0$, $100 - x - y \geq 0$) $x + y \leq 100$</p> <p>(iv) Drawing the line $2x + y = 0$ in the figure, <small>why line at</small> the least cost is attained when $x = 30$, $y = 20$. $\therefore x = 30$, $y = 20$, $z = 50$</p>	<p>1A</p> <p>1A</p> <p>1A</p> <p>1A</p> <p>1A</p> <p>1A</p> <p>1M</p> <p>1A</p>	<p>or least cost at pt.</p> <p>Any line.</p> <p>Costs at (30, 20), (80, 20), $(\frac{140}{3}, \frac{160}{3})$ are 480, 580 and 546.7 (Any point)</p>
	<u>8</u>	